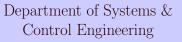
Perceptual Simplification of Paper-Based Scribbles for 3D Form Generation

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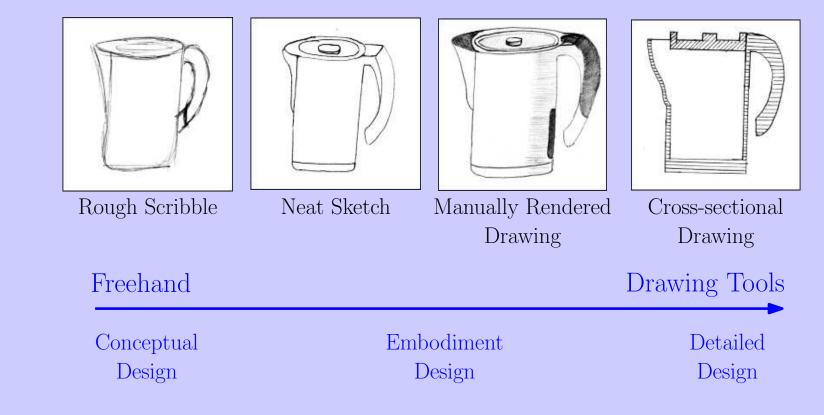






Introduction

- Traditional pen-and-paper is often the first drawing medium on which graphic ideas are expressed
- Paper-based drawings vary in detail according to the different stages of form design.

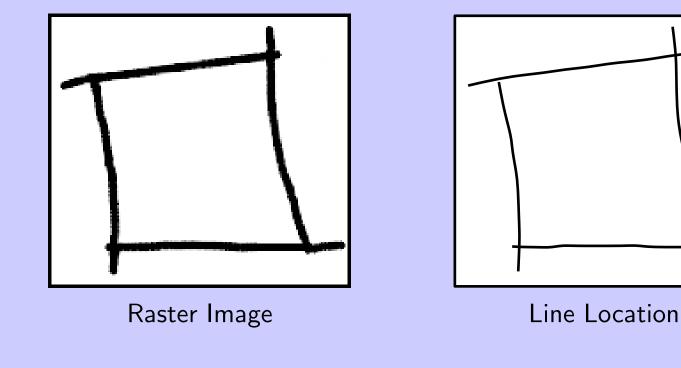


- Paper-based drawings cannot be used directly with CAD tools.
- Vectorization algorithms are generally used to convert the raster information into vector form.





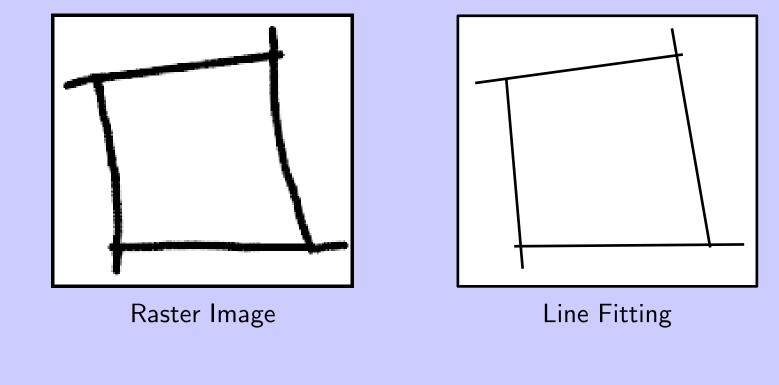
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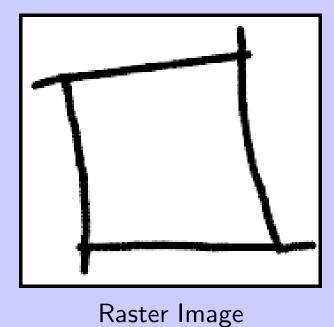
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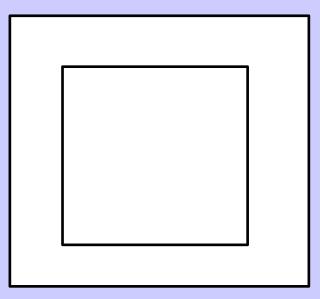
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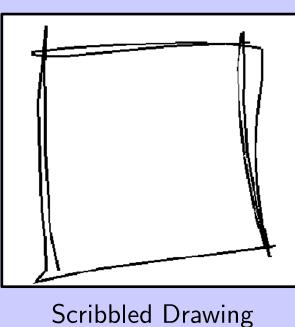


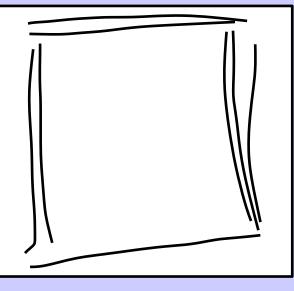


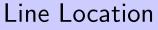




- Paper-based drawings cannot be used directly with CAD tools.
- Vectorization algorithms are generally used to convert the raster information into vector form.
- Scribbled objects **do not** have single-line edges.

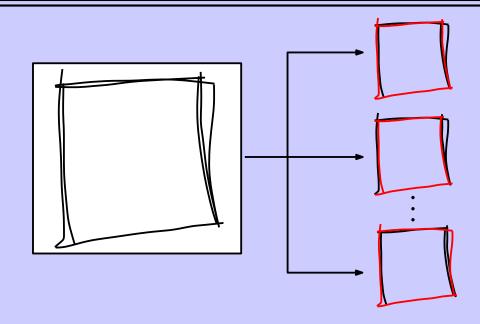








Research Problem

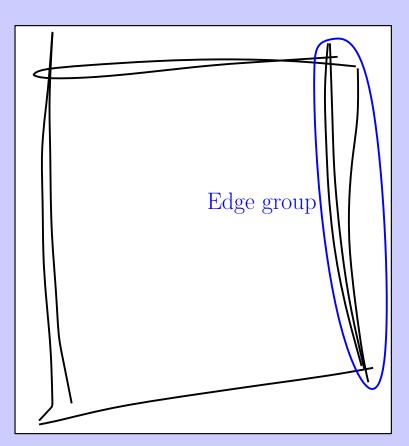


- There is no grouping algorithm that successfully groups paper-based scribble strokes.
- Existing scribble interpretation algorithms require that the scribble is drawn using 'digital ink'
 - simplifies the interpretation problem
 - digital tablets are not the designer's preferred drawing medium



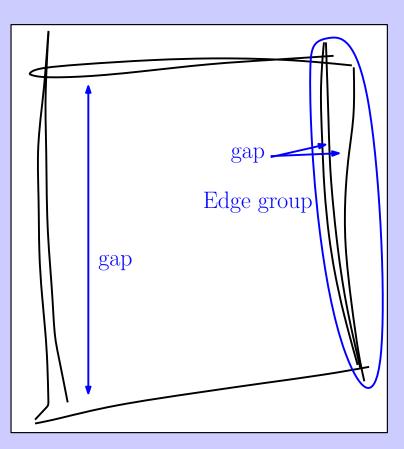
The Scribble Characteristics

- **Edge-group:** collection of strokes forming an object edge
- Intra-group gap: gap separating strokes within an edge group
- Inter-group gap: gap separating different edge groups



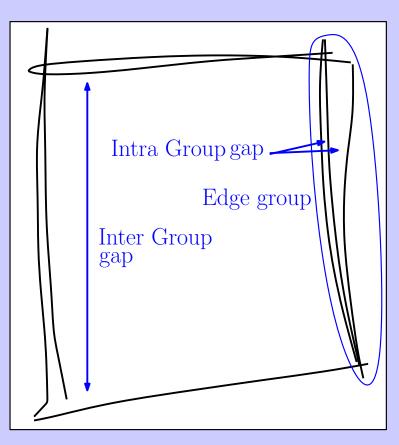
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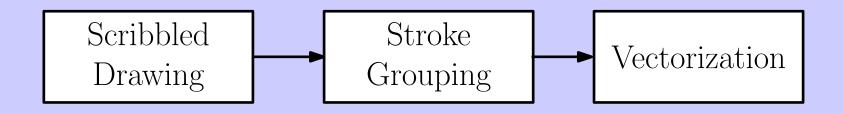
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Our Scribble Simplification Algorithm

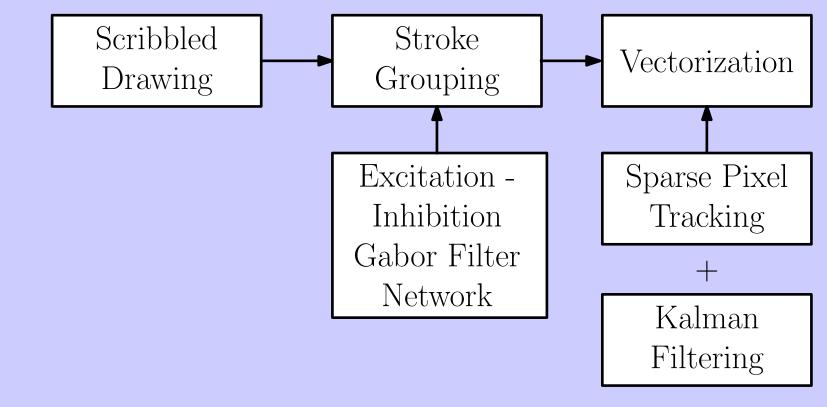
- Individual scribbled strokes gain significance only when interpreted as part of a stroke group.
- Over-strokes are grouped into line strokes before performing vectorization.





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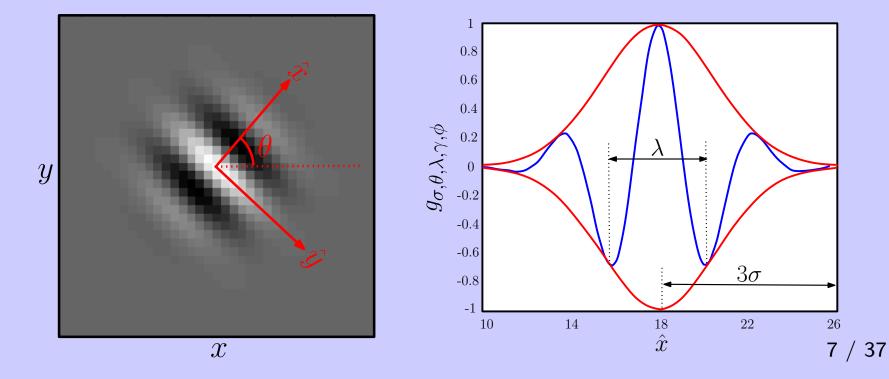


Overview of the Gabor Filter

■ The Gabor filter is defined by:

$$g_{\sigma,\theta,\lambda,\gamma,\phi}(x,y) = \exp\left\{-\frac{1}{2\sigma^2}(\hat{x}^2 + \gamma^2 \hat{y}^2)\right\} \cos\left(\frac{2\pi}{\lambda}\hat{x} + \phi\right)$$
(1)
$$\hat{x} = x\cos\theta + y\sin\theta$$
(2)
$$\hat{y} = y\cos\theta - x\sin\theta$$
(3)

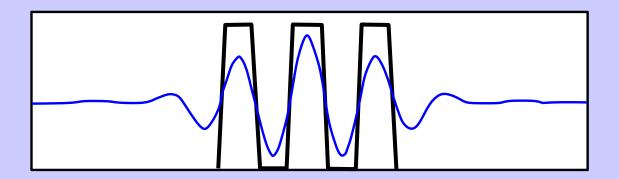
• The filter has a bandwidth $b = \log_2 \left\{ \frac{\frac{\sigma}{\lambda} + \frac{1}{\pi}\sqrt{\frac{\ln 2}{2}}}{\frac{\sigma}{\lambda} - \frac{1}{\pi}\sqrt{\frac{\ln 2}{2}}} \right\}$





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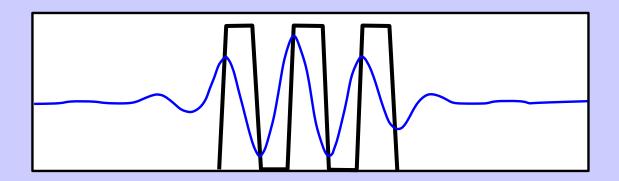
- $\blacksquare \ \phi = 0:$ filter responds to the stroke centers 'centre-on' filter
- $\blacksquare \phi = \frac{\pi}{2}$: filter responds to the stroke edges
- $\phi = \pi$: filter responds to the intra-line gaps 'centre-off' filter







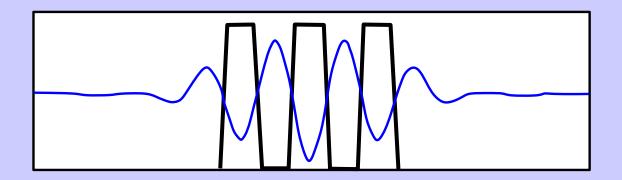
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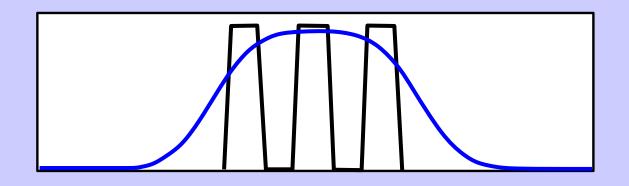


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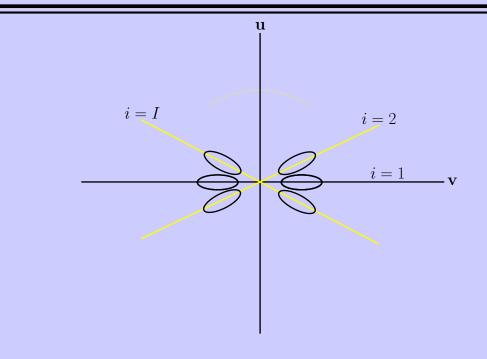




■ The energy response $G_{\theta,\lambda,\gamma}$ of a quadrature filter pair is used to give a continuous response for the stroke group

$$G_{\theta,\lambda,\gamma}(x,y) = \sqrt{\hat{g}_{\theta,\lambda,\gamma,\phi=0}^2(x,y) + \hat{g}_{\theta,\lambda,\gamma,\phi=\frac{\pi}{2}}^2(x,y)}$$
(4)

The frequency $\frac{1}{\lambda}$ and Orientation θ

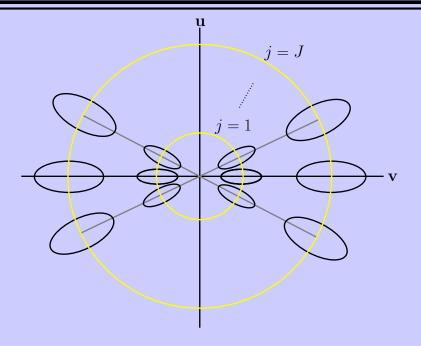


The Gabor filter bank has I orientation bands and J frequency bands which are selected such that the filter bank has complete coverage of the spatial-frequency domain



■ The Gabor filter bank implemented has 10 equally spaced orientation levels and 7 frequency levels in the range [¹/₃₀, ¹/₂] cycles per pixel for a image resolution of 72dpi

The frequency $\frac{1}{\lambda}$ and Orientation θ

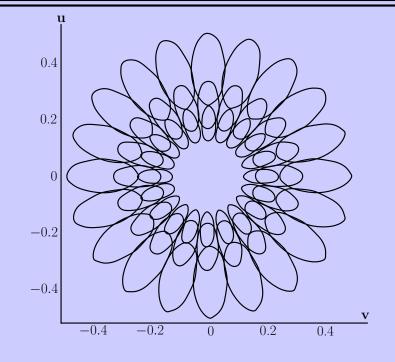


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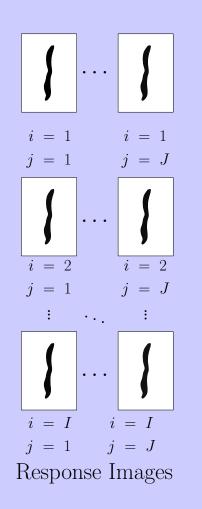
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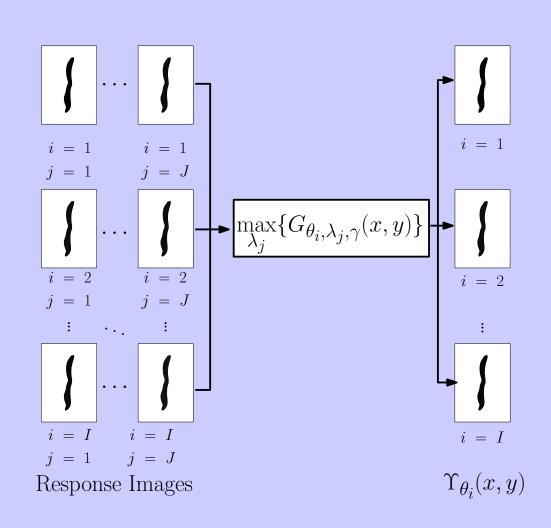


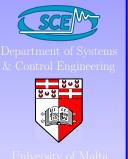


- The Gabor filter bank has I orientation bands and J frequency bands which are selected such that the filter bank has complete coverage of the spatial-frequency domain
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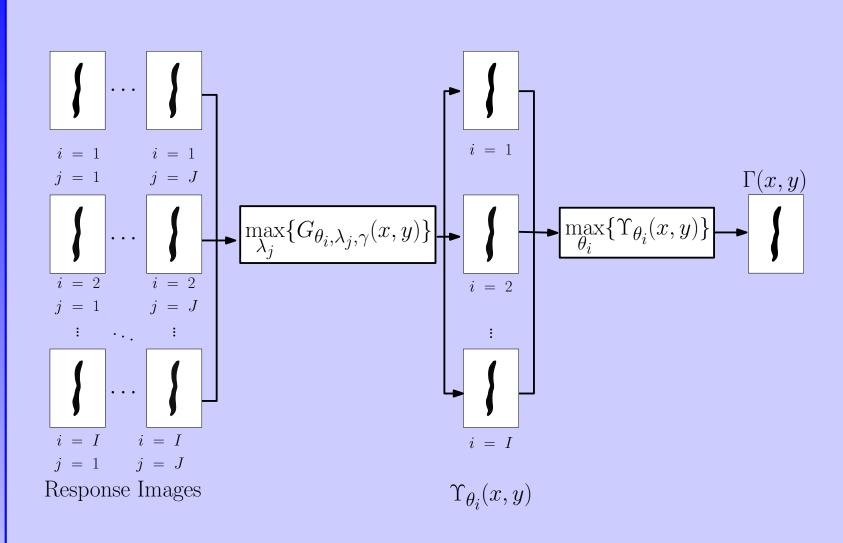






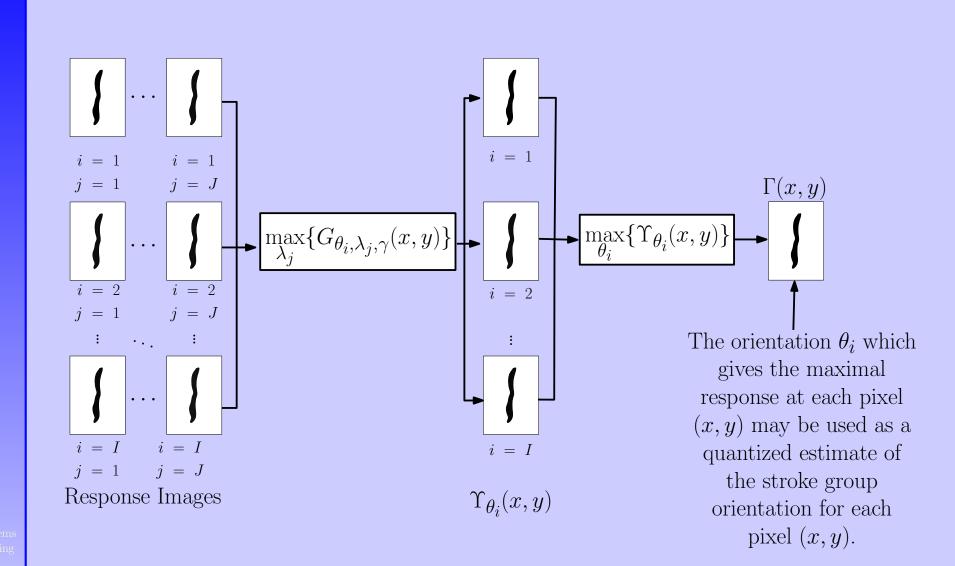


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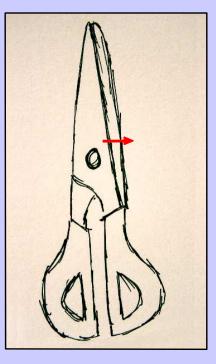


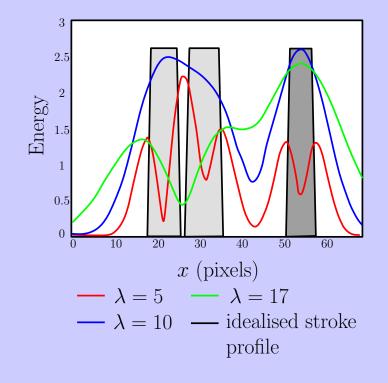
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Limitations of the Grouping Scheme

- When two or more edge groups that have a fine pattern are close to each other, the coarser filters in the filter bank respond to the edge groups as a single coarse pattern.
- This will not allow the quadrature grouping scheme to make sufficient distinction between edge-groups.



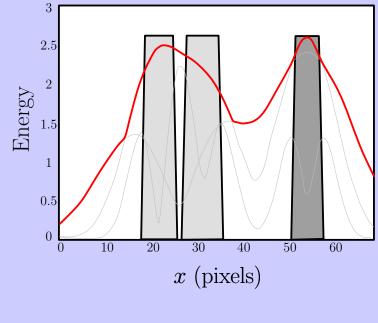




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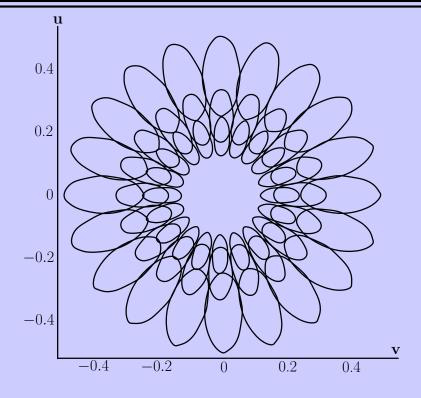






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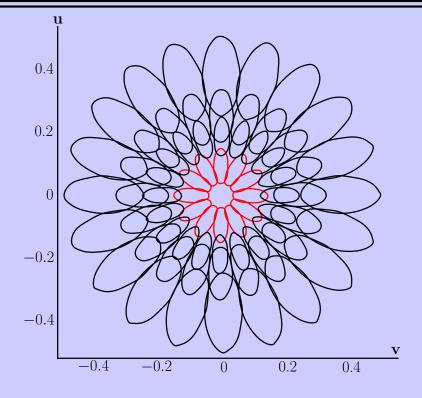
The Inhibiting Filter





- The visual pattern formed by two edge groups and the inter-group gap has a lower frequency than the pattern formed by the strokes within the edge groups.
- To inhibit the inter-group gaps the filter must give a positive response at the gaps, hence it requires a phase of $\phi = \pi$

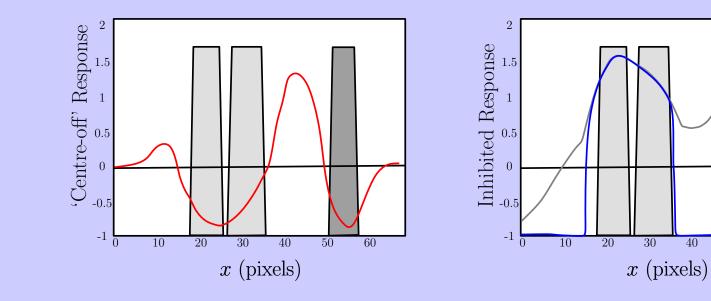
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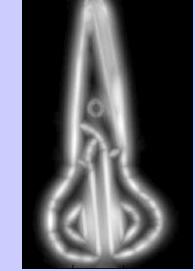




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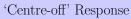
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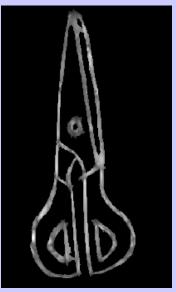












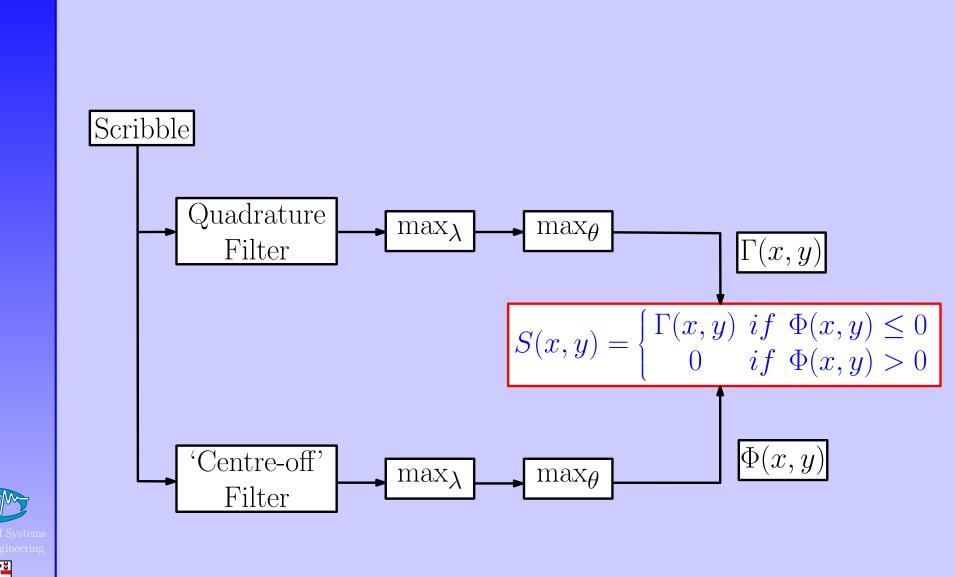
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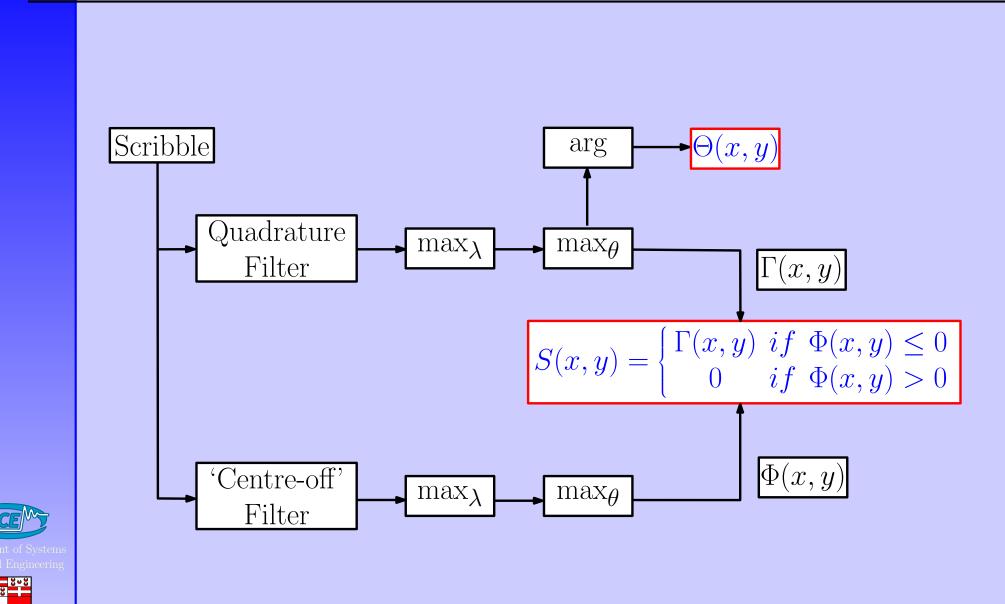


The Stroke Grouping Algorithm





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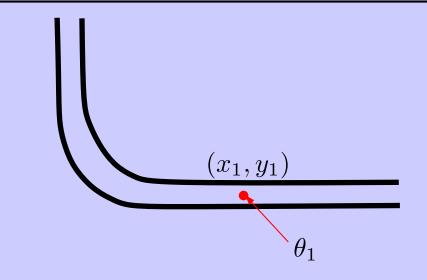
New vs 'Off-the-Shelf' Vectorization

- The Gabor-grouping algorithm simplifies the scribbled drawing creating a new raster image in which
 - ◆ edge groups are represented by single lines
 - the edge groups have a line width greater than unity
- Therefore the simplified scribble must be processed with a vectorization algorithm similar to those proposed for neat paper-based drawings
- The Gabor-grouping algorithm augments the scribbled drawing with quantized estimates of the stroke orientations



These orientations are used to guide a line tracking algorithm and hence replace the line location step used in these vectorization algorithms

The Line Tracking Algorithm



■ Using the orientation θ_k at a tracking instant k the position of the track point for the next tracking instant k + 1 may be predicted using

$$x_{k+1} = x_k + D\cos(\theta_k)$$

$$y_{k+1} = y_k + D\sin(\theta_k)$$
(5)
(6)



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The Line Tracking Algorithm

$$x_{2} = x_{1} + D\cos(\theta_{1})$$

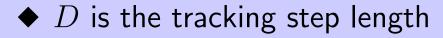
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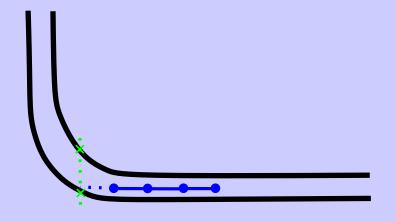
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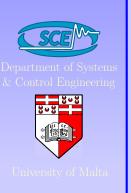
This piece-wise linear tracking may be offset from the actual medial points



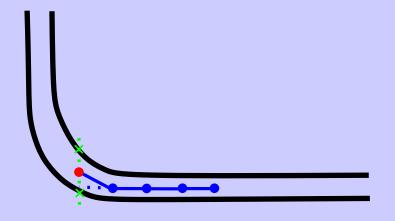
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- To compensate for this offset, an oriented scan line is taken at each new point to determine the contour boundaries of the line segment



The Line Tracking Algorithm

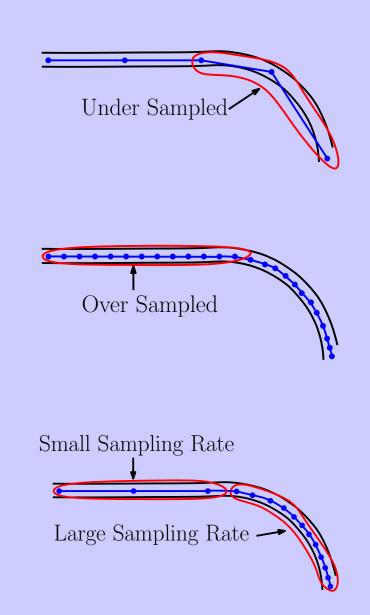


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The midpoint of the scan line is used as a better estimate of the medial point

- The tracking algorithm should not under sample or over sample the drawing
- Since the drawings may contain a mixture of straight line segments and curved segments an adaptive tracking step is required.
- A straight line segments are detected when the tacking point remains on the stroke foreground and the orientation remains constant
- Curved segments are detected when the orientation of subsequent tracking points changes

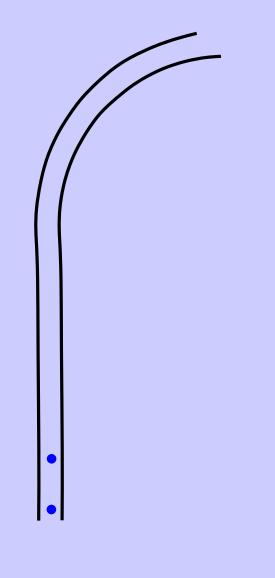




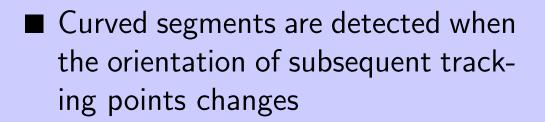
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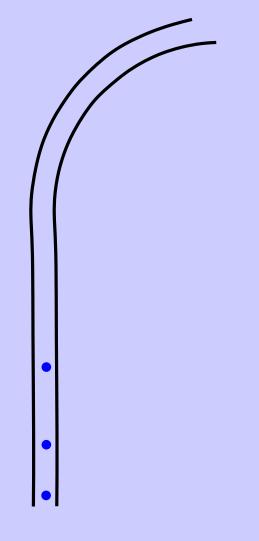


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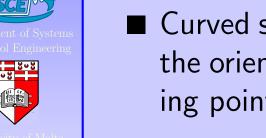
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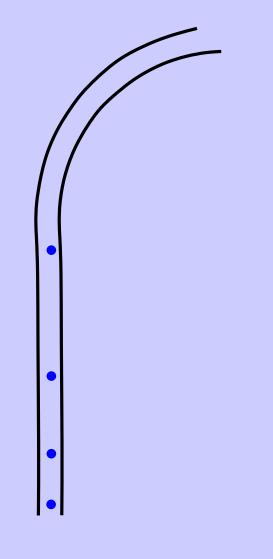




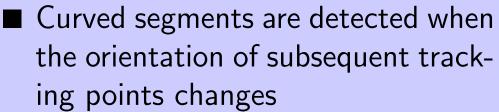
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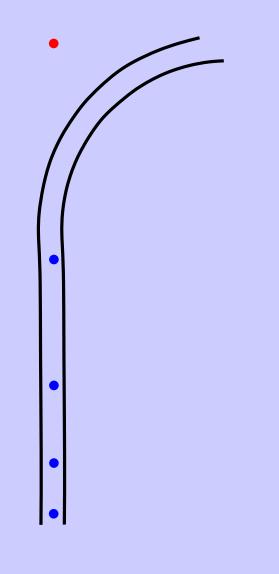


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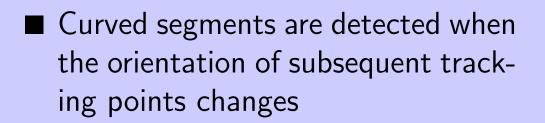
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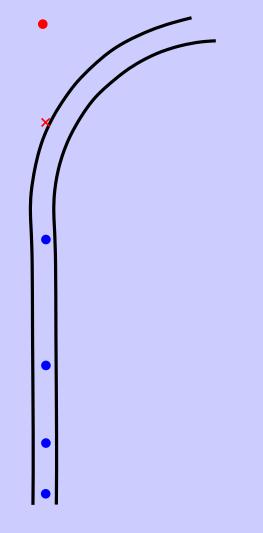






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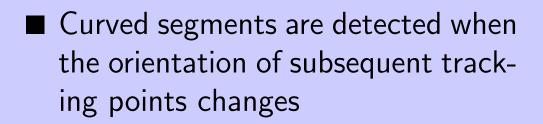


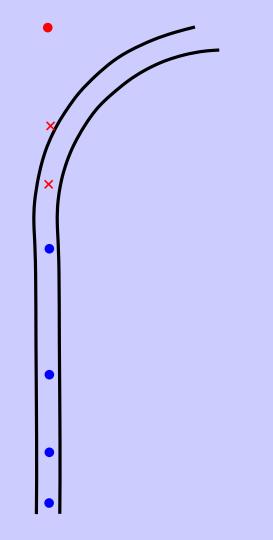




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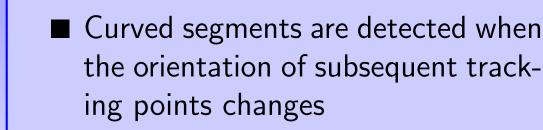
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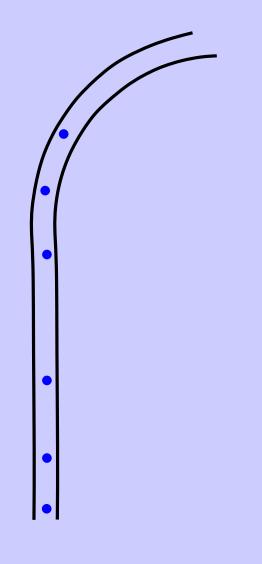




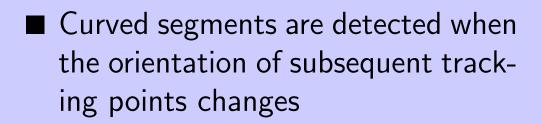


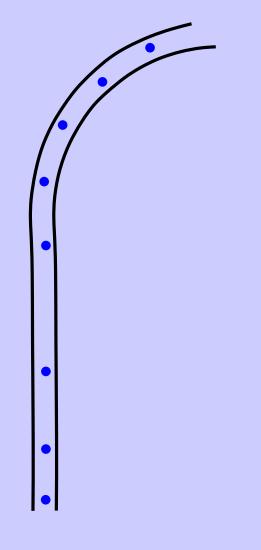
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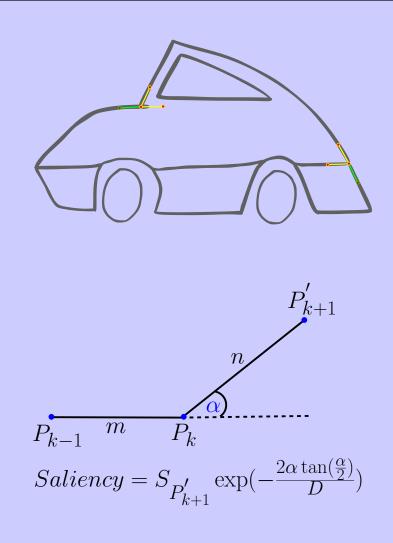
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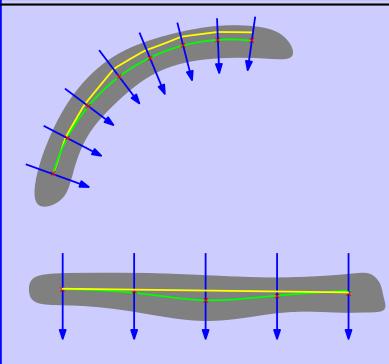


Salient Point Tracking at Junctions



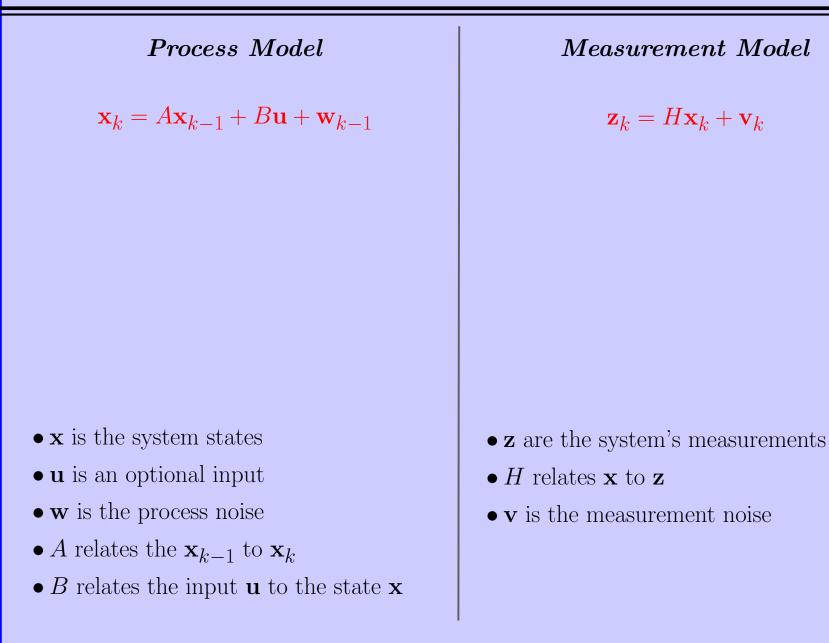
- At junctions, the tracking algorithm should select the path that gives maximum saliency
- The local saliency is measured by propagating the line path to a preliminary track point P'_{k+1}
- The direction which results in maximum local saliency is selected as the tracking direction

Introducing the Kalman Filter



- Line boundary midpointsPiece-wise Linear Tracking
- → Oriented Scan line

- The tracking algorithm has two medial point estimates
- The piecewise linear tracking is not suitable for high curvatures
- The contour boundaries are not suitable for lines with contour boundary noise
- A mechanism that obtains a better estimate from these two estimates is required
- The Kalman filter is introduced to the line tracking algorithm to provide this mechanism



Process Model $\mathbf{x}_{k} = A\mathbf{x}_{k-1} + B\mathbf{u} + \mathbf{w}_{k-1}$ $x_{k} = x_{k-1} + D\cos(\theta_{k-1})$ $y_{k} = y_{k-1} + D\sin(\theta_{k-1})$ $\begin{pmatrix} x \\ y \end{pmatrix}_{k} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}_{k-1} + \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} D\cos\theta \\ D\sin\theta \end{pmatrix}$

- $\bullet \ {\bf x}$ is the system states
- $\bullet \ \mathbf{u}$ is an optional input
- $\bullet \ {\bf w}$ is the process noise
- A relates the \mathbf{x}_{k-1} to \mathbf{x}_k
- $\bullet \, B$ relates the input ${\bf u}$ to the state ${\bf x}$

Measurement Model

$$\mathbf{z}_k = H\mathbf{x}_k + \mathbf{v}_k$$

- $\bullet \ {\bf z}$ are the system's measurements
- $\bullet \, H$ relates ${\bf x}$ to ${\bf z}$
- $\bullet \ {\bf v}$ is the measurement noise

Process Model $\mathbf{x}_{k} = A\mathbf{x}_{k-1} + B\mathbf{u} + \mathbf{w}_{k-1}$ $x_{k} = x_{k-1} + D\cos(\theta_{k-1})$ $y_{k} = y_{k-1} + D\sin(\theta_{k-1})$ $\begin{pmatrix} x \\ y \end{pmatrix}_{k} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}_{k-1} + \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} D\cos\theta \\ D\sin\theta \end{pmatrix}$

- $\bullet \ {\bf x}$ is the system states
- $\bullet \ \mathbf{u}$ is an optional input
- $\bullet \ {\bf w}$ is the process noise
- A relates the \mathbf{x}_{k-1} to \mathbf{x}_k
- $\bullet \, B$ relates the input ${\bf u}$ to the state ${\bf x}$

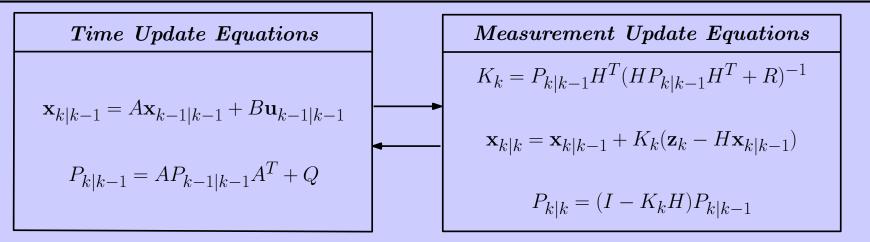
Measurement Model

$$\mathbf{z}_k = H\mathbf{x}_k + \mathbf{v}_k$$

$$z_{x_k} = x_k$$
$$z_{y_k} = y_k$$

$$\begin{pmatrix} z_x \\ z_y \end{pmatrix}_k = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}_k$$

- z are the system's measurements
- H relates \mathbf{x} to \mathbf{z}
- $\bullet \ {\bf v}$ is the measurement noise

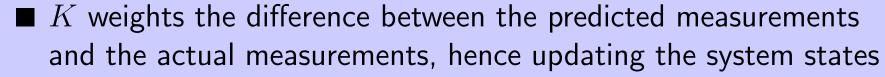


 $\blacksquare Q$ is the covariance of the process noise ${\bf w}$

- $\blacksquare R$ is the covariance of measurement noise ${\bf v}$
- \blacksquare *P* is the error covariance



K is a gain matrix which minimizes the *a posteriori* error covariance.



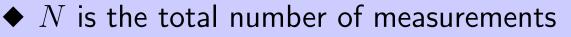
The Smoothed Kalman Filter

- Since the Kalman filter acts upon the system in a forward manner, the estimation of the system states using the Kalman filter is causal.
- To remove this causality, the forward estimation is augmented to include a Kalman smoothing step

$$J_{k|N} = P_{k|k}A^{T}(P_{k+1|k}^{-1})$$

$$\mathbf{x}_{k|N} = \mathbf{x}_{k|k} + J_{k}(\mathbf{x}_{k+1|N} - A\mathbf{x}_{k|k})$$

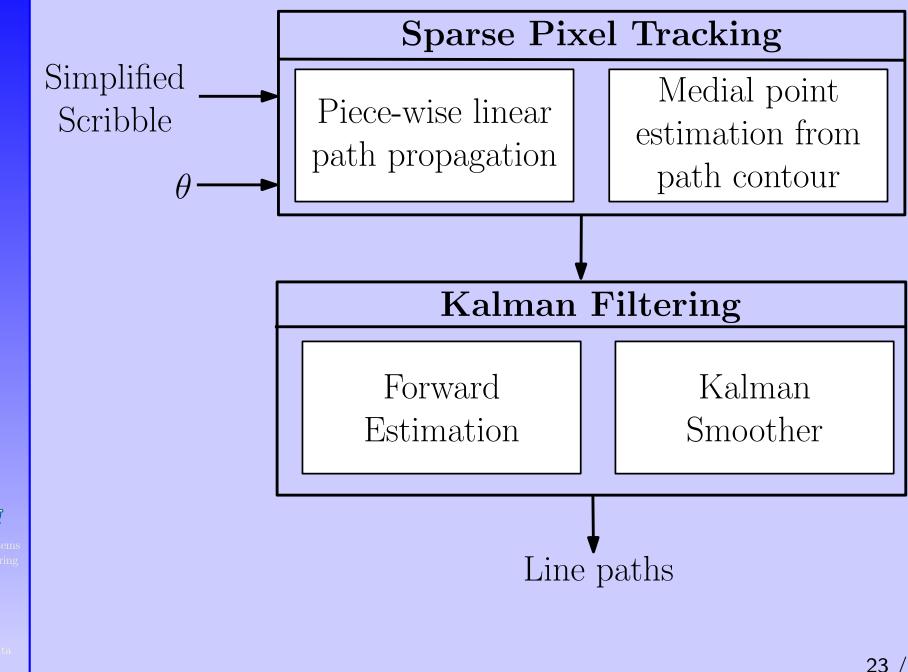
$$P_{k|N} = P_{k|k} + J_{k}(P_{k+1|N} - P_{k+1|k})J_{k}^{-1}$$



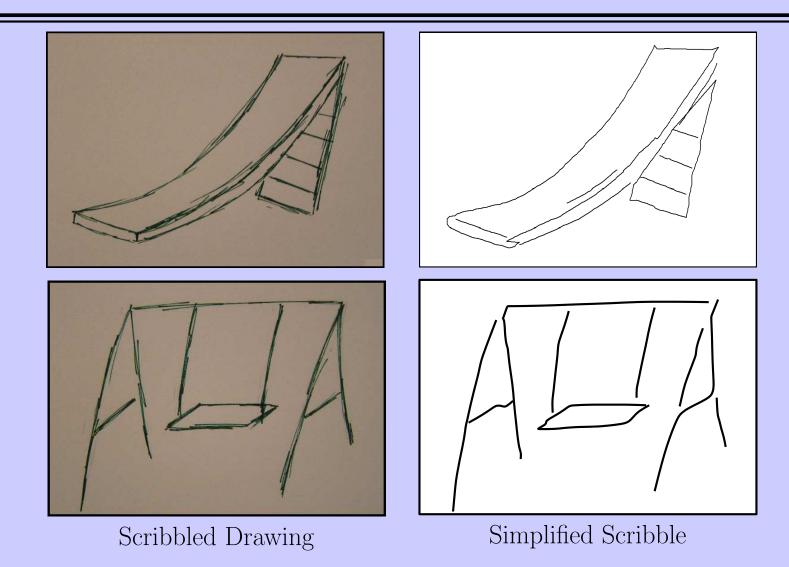
◆ The smoothed states x are estimated using backward recursions k = N, N − 1, · · · , 1 conditioned on all the measurement data z_{1:N}



The Line Location Algorithm



Results







Comparison of the Gabor Grouping Algorithm with Morphology Operators

	Scribble	'Close' Operation			Gabor
Image ID	Roughness	W = 5	W = 9	W = 11	Filtering
Test 1	49.94	39.89	35.59	32.63	21.22
Test 2	10.44	23.57	23.58	23.59	13.57
Test 3	45.66	34.31	33.41	33.97	19.46
Test 4	41.99	25.07	23.92	23.43	9.97
Test 5	40.04	28.52	26.01	26.03	22.88
Test 6	50.24	37.17	32.42	33.47	17.69
$-\mu$	43.68	32.13	29.87	28.95	18.48
σ	6.61	7.71	7.89	8.26	5.56





Comparing the total number of pixels that do not match with the ground truth drawing

Evaluation of Results

EVALUATING THE USEFULNESS OF THE GABOR GROUPING ALGORITHM

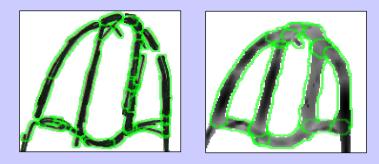


Image ID	Ground Truth	Scribble	Simplified Scribble
Test 1	18	53	18
Test 2	13	44	18
Test 3	14	44	15
Test 4	15	64	16
Test 5	9	50	13
Test 6	22	62	24

Comparing the number of segments obtained by the ScanScribe software for the ground truth drawing,

the scribbled drawing and the simplified drawing

Comparison of the Proposed Line Tracking Algorithm and the Sparse Pixel Vectorization Algorithm on Neat Line Drawings

SPV

0.87

0.82

0.81

Kalman Tracking

0.90

0.86

0.92

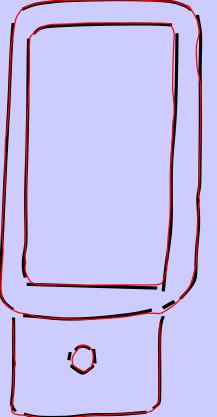
0.88

0.87

0.88

0.87

0.02



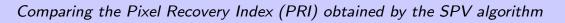
	0.01	
Test 4	0.76	
Test 5	0.80	
Test 6	0.82	
 μ	0.82	
σ	0.03	

Image ID

Test 1

Test 2

Test 3

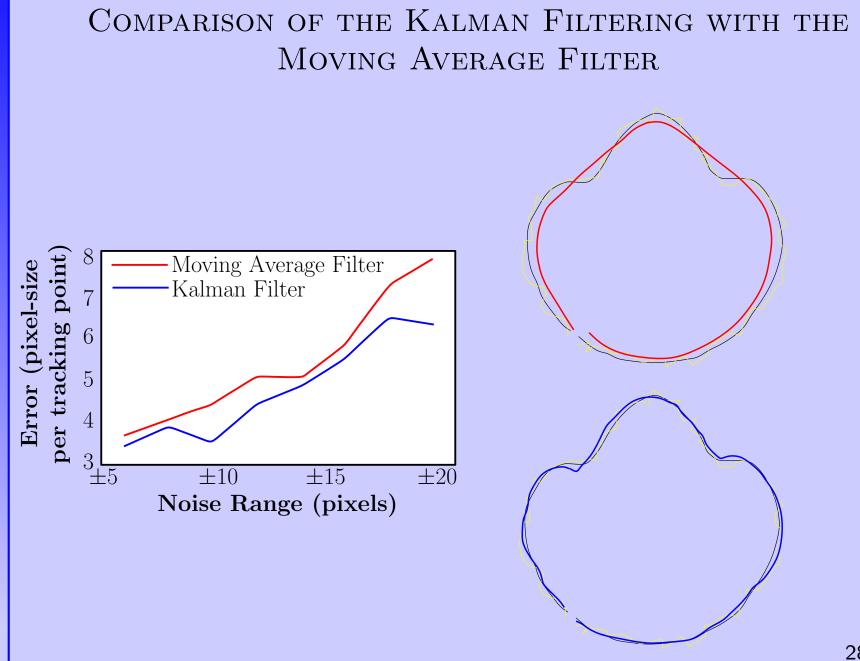


and the proposed line tracking algorithm



Proposed AlgorithmSPV Algorithm

Evaluation of Results



Obtaining 3D Form from Scribbles

- The medial points obtained from our algorithm can be used directly in CAD tools. However, the CAD representation would still be a 2D representation and further CAD operations are required to obtain the 3D form.
- We have proposed an annotation language whereby the scribbled drawing can be annotated in an intuitive way so as to allow computer algorithms to automatically obtain the 3D form form the paper-based drawing.



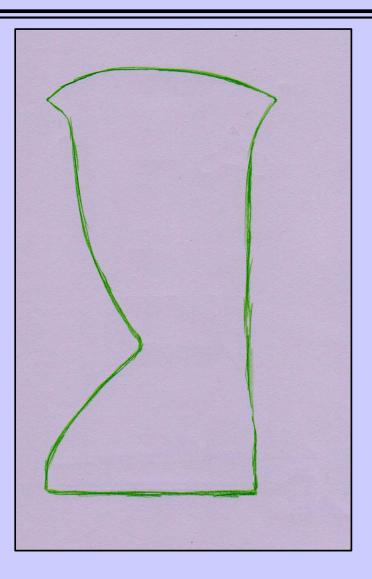
The Components of the Annotation Language

■ A complete and annotated sketch will consist of

Object profile: a sketch depicting a side view of the object
 Plane lines: lines that indicate planes of interest in the object
 Cross-sectional profiles: 2D sketches that indicate the cross-sectional shape of the object

The object profile must be drawn in a different colour than the plane lines and cross-sectional profiles

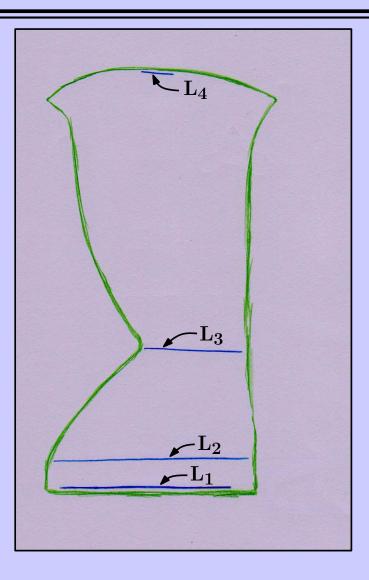




1. Sketch the object profile.

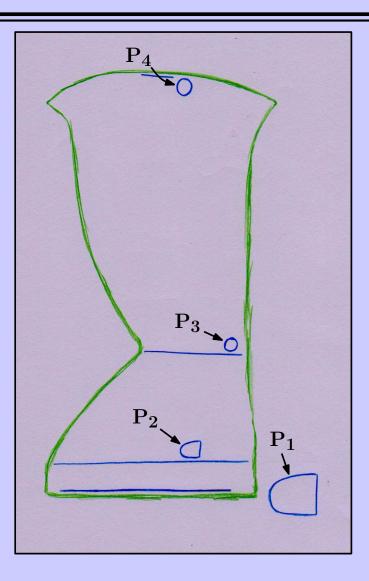


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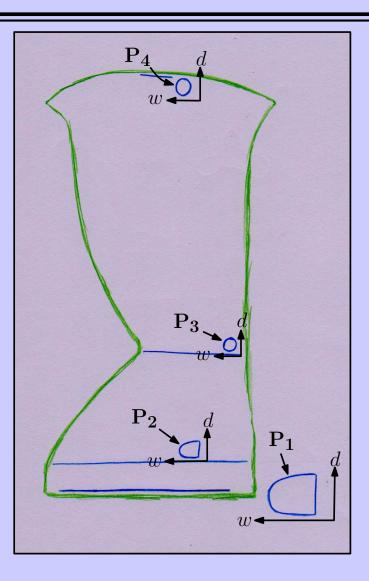
2. Mark salient planes with a plane line.







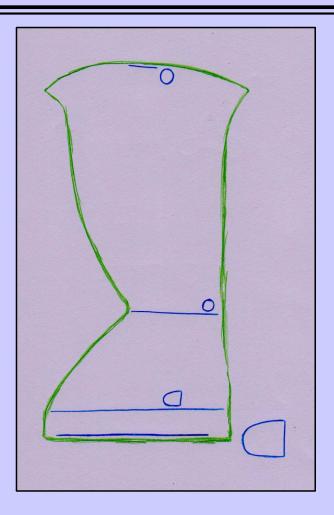
3. Use cross-sectional profiles to specify the cross-sectional shape at the plane lines.





3. Use cross-sectional profiles to specify the cross-sectional shape at the plane lines.

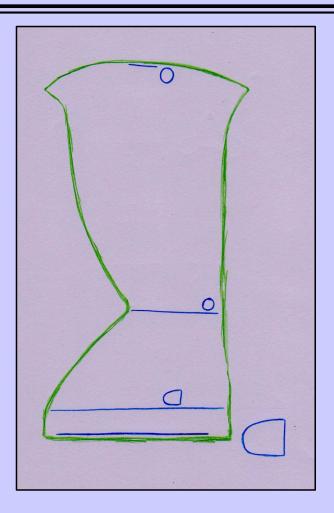
Case Study 1: Interpreting the Sketch





Centre and scale the given cross-sectional profiles

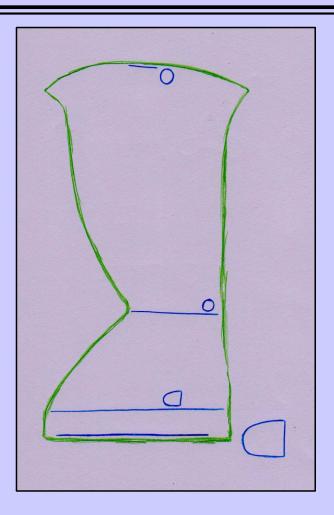
Case Study 1: Interpreting the Sketch





- Centre and scale the given cross-sectional profiles
- Create intermediary cross-sectional profiles to define the object form accurately

Case Study 1: Interpreting the Sketch

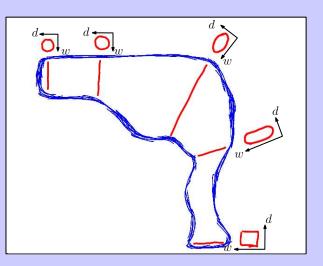




Centre and scale the given cross-sectional profiles

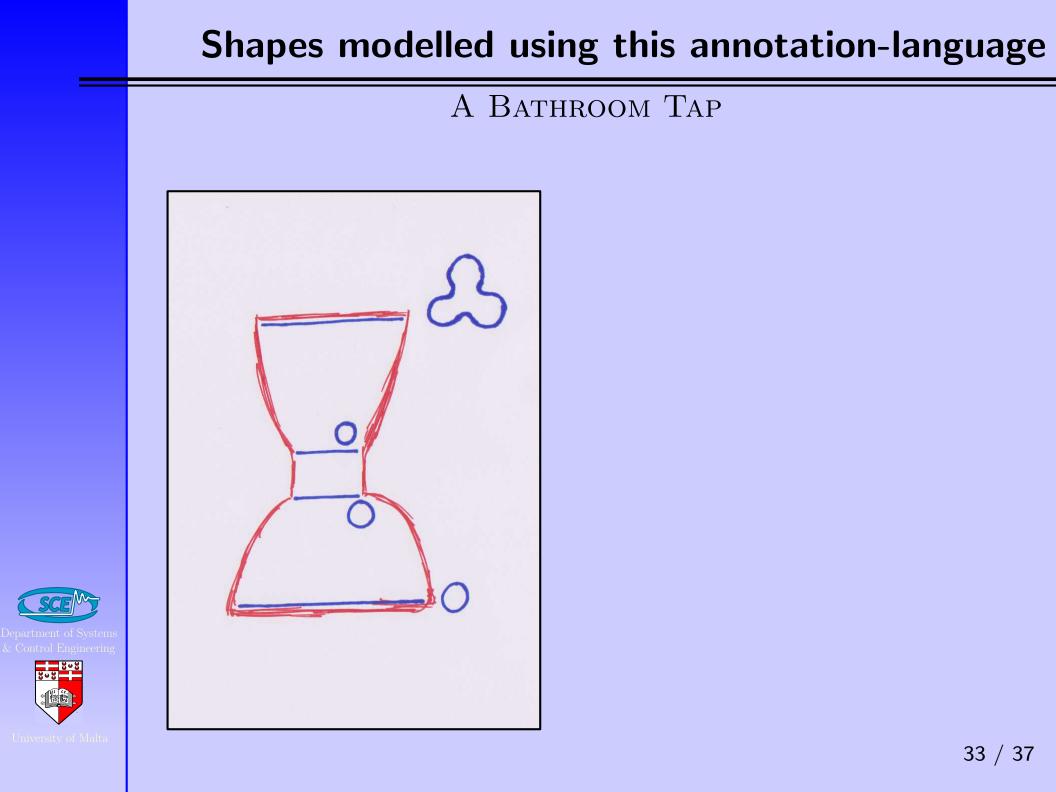
Shapes modelled using this annotation-language

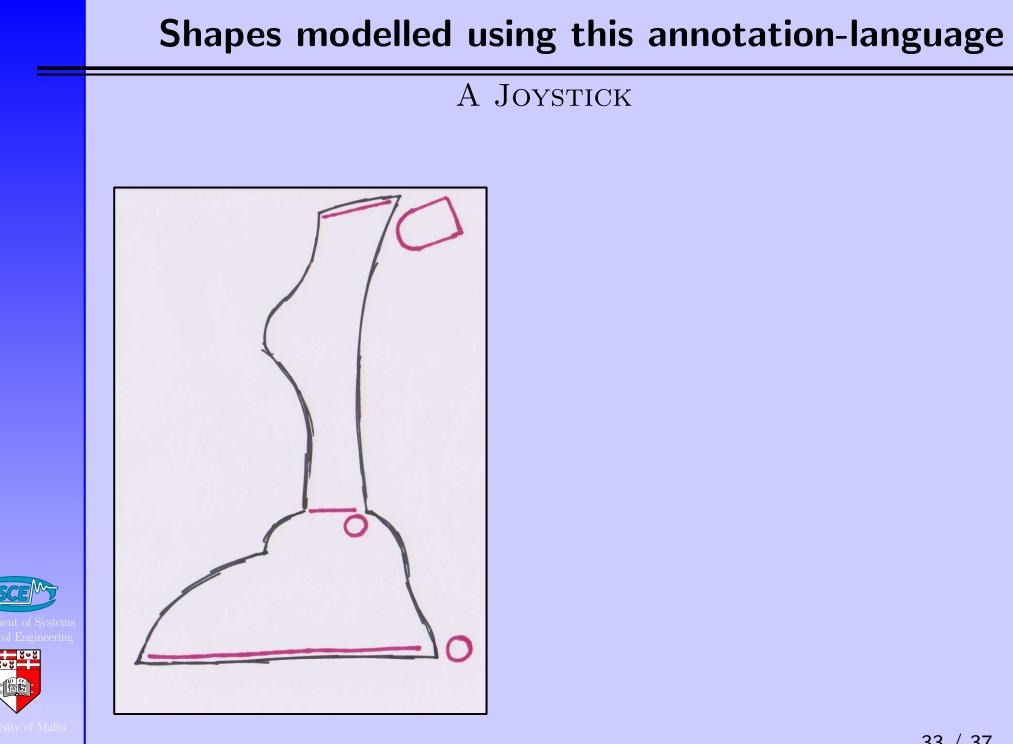
A HAIR DRYER





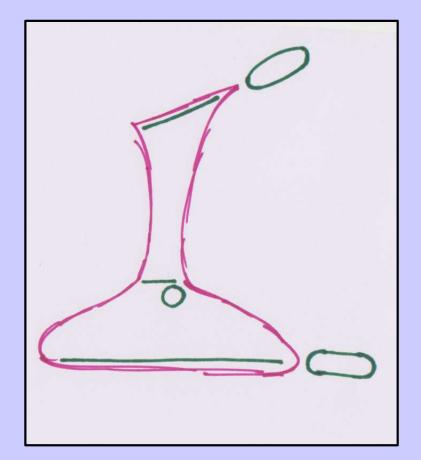






Shapes modelled using this annotation-language

A NAIL POLISH BOTTLE

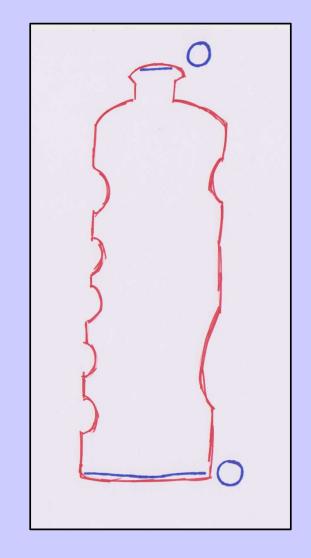






Shapes modelled using this annotation-language

An 'Easy Grip' Drinking Flask



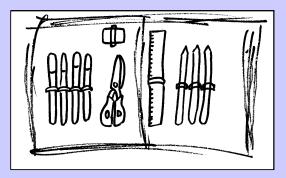




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Conclusions

- These algorithms make CAD tools accessible from scribbled drawings, thus decreasing the time taken for a designer to obtain virtual prototypes from concept drawings.
- Our algorithms can be further improved in order to successfully interpret different genres of scribbles. This involves:
 - Simplification of scribbles having different stroke resolutions





 Improving the annotation language to cater for more complex forms involving different parts

List of Publications

- 1. Bartolo A., Farrugia P., Camilleri K. P., Borg J. C., A Profile-driven Sketching Interface for Pen-and-Paper Sketches in Proceedings of the Workshop on Sketch Tools for diagramming, Herrshing am Ammersee, Germany, 2008
- 2. Bartolo A., Camilleri K. P., Fabri S. G., Borg J. C., Paper-based Scribble Simplification: Where Do We Stand? in Proceedings of the Eurographics Workshop on Sketch-Based Interfaces and Modeling 2008, pg. 25-32
- 3. Bartolo A., Camilleri K. P., Fabri S. G., Borg J.C., Line Tracking Algorithm for Scribbled Drawings. In Proceedings of the 3rd International Symposium on Communications, Control and Signal Processing, 2008
- 4. Bartolo A., Camilleri K.P., Fabri S. G., Borg J.C., Farrugia P.J. Scribbles to Vectors: Preparation of Scribble Drawings for CAD Interpretation. In Proceedings of the Eurographics Workshop on Sketch-Based Interfaces and Modeling 2007.
- 5. Bartolo A., Cassar T., Camilleri K.P, Fabri S.G., Borg J. C. Image Binarization using the Extended Kalman Filter. Informatics in Control, Automation and Robotics II, pp 153-162, J. Filipe, J.L. Ferriera, J. A. Cetto and M. Carvalho editors, Springer 2006
- 6. Bartolo A., Camilleri K.P., Farrugia P.J., Borg J.C. A New Sketch Based Interface using the Gray-level Co-occurrence Matrix for Perceptual Simplification of Paper Based Scribbles. In Proceedings of the Eurographics Workshop on Sketch-Based Interfaces and Modeling, pp 91 - 98, 2006
- Bartolo A., Cassar T., Camilleri K.P, Fabri S.G., Borg J. C. Image Binarization using the Extended Kalman Filter. In Proceedings of the 2nd International Conference on Informatics in Control, Automation and Robotics Vol. 2 pp 160-167, 2005



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Further information on the research work carried out within the Department of Systems and Control Engineering can be accessed at http://www.um.edu.mt/eng/sce

